

# Ionizing Radiation

## Chapter 1

F.A. Attix, Introduction to Radiological  
Physics and Radiation Dosimetry

## Outline

- Radiological physics and radiation dosimetry
- Types and sources of ionizing radiation
- Description of ionizing radiation fields
  - Random nature of radiation
  - Non-stochastic quantities

## Introduction

- Radiological physics studies ionizing radiation and its interaction with matter
- Began with discovery of x-rays, radioactivity and radium in 1890s
- Special interest is in the energy absorbed in matter
- Radiation dosimetry deals with quantitative determination of the energy absorbed in matter

## Ionizing radiation

- By general definition ionizing radiation is characterized by its ability to excite and ionize atoms of matter
- Lowest atomic ionization energy is  $\sim$  eV, with very little penetration
- Energies relevant to radiological physics and radiation therapy are in keV – MeV range

## Types and sources of ionizing radiation

- $\gamma$ -rays: electromagnetic radiation (photons) emitted from a nucleus or in annihilation reaction
  - Practical energy range from 2.6 keV ( $K_{\alpha}$  from electron capture in  $^{37}_{18}\text{Ar}$ ) to 6.1 and 7.1 MeV ( $\gamma$ -rays from  $^{16}_7\text{N}$ )
- x-rays: electromagnetic radiation (photons) emitted by charged particles (characteristic or bremsstrahlung processes). Energies:
  - 0.1-20 kV “soft” x-rays
  - 20-120 kV diagnostic range
  - 120-300 kV orthovoltage x-rays
  - 300 kV-1 MV intermediate energy x-rays
  - 1 MV and up megavoltage x-rays

## Types and sources of ionizing radiation

- Fast electrons (positrons) emitted from nuclei ( $\beta$ -rays) or in charged-particle collisions ( $\delta$ -rays). Other sources: Van de Graaf generators, linacs, betatrons, and microtrons
- Heavy charged particles emitted by some radioactive nuclei ( $\alpha$ -particles), cyclotrons, heavy particle linacs (protons, deuterons, ions of heavier elements, etc.)
- Neutrons produced by nuclear reactions (cannot be accelerated electrostatically)

## Types of interaction

- ICRU (The *International Commission on Radiation Units and Measurements*; established in 1925) terminology
- *Directly ionizing radiation*: by charged particles, delivering their energy to the matter directly through multiple Coulomb interactions along the track
- *Indirectly ionizing radiation*: by photons (x-rays or  $\gamma$ -rays) and neutrons, which transfer their energy to charged particles (two-step process)

## Description of ionizing radiation fields

- To describe radiation field at a point P need to define non-zero volume around it
- Can use *stochastic* or *non-stochastic* physical quantities

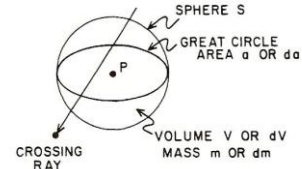


FIGURE 1.1. Characterizing the radiation field at a point P in terms of the radiation traversing the spherical surface S.

## Stochastic quantities

- Values occur randomly, cannot be predicted
- Radiation is random in nature, associated physical quantities are described by probability distributions
- Defined for finite domains (non-zero volumes)
- The *expectation value* of a stochastic quantity (e.g., number of x-rays detected per measurement) is the mean of its measured value for infinite number of measurements

$$\bar{N} \rightarrow N_e \text{ for } n \rightarrow \infty$$

## Stochastic quantities

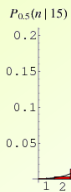
- For a “constant” radiation field a number of x-rays observed at point P per unit area and time interval follows Poisson distribution
- For large number of events it may be approximated by normal (Gaussian) distribution, characterized by standard deviation  $\sigma$  (or corresponding percentage standard deviation S) for a single measurement

$$\sigma = \sqrt{N_e} \cong \sqrt{\bar{N}}$$

$$S = \frac{100\sigma}{N_e} = \frac{100}{\sqrt{N_e}} \cong \frac{100}{\sqrt{\bar{N}}}$$

## Stochastic quantities

- Normal (Gaussian) distribution is described by probability density function  $P(x)$
- Mean  $\bar{N}$  determines position of the maximum, standard deviation  $\sigma$  defines the width of the distribution



$$P(N) = \frac{1}{\sigma\sqrt{2\pi}} e^{-\frac{(N-\bar{N})^2}{2\sigma^2}}$$

## Stochastic quantities

- For a given number of measurements  $n$  standard deviation is defined as

$$\sigma' = \frac{\sigma}{\sqrt{n}} = \sqrt{\frac{N_e}{n}} \cong \sqrt{\frac{\bar{N}}{n}}$$

$$S' = \frac{100\sigma'}{N_e} = \frac{100}{\sqrt{nN_e}} \cong \frac{100}{\sqrt{n\bar{N}}}$$

- $\bar{N}$  will have a 68.3% chance of lying within interval  $\pm\sigma'$  of  $N_e$ , 95.5% to be within  $\pm 2\sigma'$ , and 99.7% to be within interval  $\pm 3\sigma'$ . No experiment-related fluctuations

## Stochastic quantities

- In practice one always uses a detector. An estimated precision (proximity to  $N_e$ ) of any single random measurement  $N_i$

$$\sigma \cong \left[ \frac{1}{n-1} \sum_{i=1}^n (N_i - \bar{N})^2 \right]^{1/2}$$

$$\bar{N} = (\sum N_i) / n$$

- Determined from the data set of  $n$  such measurements

## Stochastic quantities

- An estimate of the precision (proximity to  $N_e$ ) of the mean value  $\bar{N}$  measured with a detector  $n$  times

$$\sigma' = \sigma / \sqrt{n}$$

$$\sigma' \cong \left[ \frac{1}{n(n-1)} \sum_{i=1}^n (N_i - \bar{N})^2 \right]^{1/2}$$

- $N_e$  is as correct as your experimental setup

## Stochastic quantities: Example

- A  $\gamma$ -ray detector having 100% counting efficiency is positioned in a constant field, making 10 measurements of equal duration,  $\Delta t = 100$ s (exactly). The average number of rays detected ("counts") per measurement is  $1.00 \times 10^5$ . What is the mean value of the count rate  $C$ , including a statement of its precision (i.e., standard deviation)?

$$\bar{C} = \frac{\bar{N}}{\Delta t} = \frac{1.00 \times 10^5}{100} = 1.00 \times 10^3 \text{ c/s}$$

$$\sigma'_c \cong \sqrt{\frac{\bar{C}}{n}} = \sqrt{\frac{1.00 \times 10^3}{10}} = 1 \text{ c/s}$$

$$\bar{C} = 1.00 \times 10^3 \pm 1 \text{ c/s}$$

- Here the standard deviation is due entirely to the stochastic nature of the field, since detector is 100% efficient

## Non-stochastic quantities

- For given conditions the value of non-stochastic quantity can, in principle, be calculated
- In general, it is a "point function" defined for infinitesimal volumes
  - It is a continuous and differentiable function of space and time; with defined spatial gradient and time rate of change
- Its value is equal to, or based upon, the *expectation value* of a related stochastic quantity, if one exists
  - In general does not need to be related to stochastic quantities, they are related in description of ionizing radiation

## Description of radiation fields by non-stochastic quantities

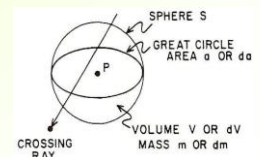
- Fluence
- Flux Density (or Fluence Rate)
- Energy Fluence
- Energy Flux Density (or Energy Fluence Rate)

## Non-stochastic quantities: Fluence

- A number of rays crossing an infinitesimal area surrounding point  $P$ , define fluence as

$$\Phi = \frac{dN_e}{da}$$

- Units of  $m^2$  or  $cm^2$



## Non-stochastic quantities: Flux density (Fluence rate)

- An increment in fluence over an infinitesimally small time interval

$$\phi = \frac{d\Phi}{dt} = \frac{d}{dt} \left( \frac{dN_e}{da} \right)$$

- Units of  $\text{m}^{-2} \text{s}^{-1}$  or  $\text{cm}^{-2} \text{s}^{-1}$
- Fluence can be found through integration:

$$\Phi(t_0, t_1) = \int_{t_0}^{t_1} \phi(t) dt$$

## Non-stochastic quantities: Energy fluence

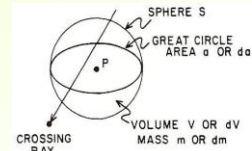
- For an expectation value  $R$  of the energy carried by all the  $N_e$  rays crossing an infinitesimal area surrounding point  $P$ , define energy fluence as

$$\Psi = \frac{dR}{da}$$

- Units of  $\text{J m}^{-2}$  or  $\text{erg cm}^{-2}$
- If all rays have energy  $E$

$$R = EN_e$$

$$\Psi = E\Phi$$



## Differential distributions

- More complete description of radiation field is often needed
- Generally, flux density, fluence, energy flux density, or energy fluence depend on all variables:  $\theta$ ,  $\beta$ , or  $E$
- Simpler, more useful differential distributions are those which are functions of only one of the variables

## Differential distributions by energy and angle of incidence

- Differential flux density as a function of energy and angles of incidence: distribution

$$\phi'(\theta, \beta, E)$$

- Typical units are  $\text{m}^{-2} \text{s}^{-1} \text{sr}^{-1} \text{keV}^{-1}$
- Integration over all variables gives the flux density:

$$\phi = \int_{\theta=0}^{\pi} \int_{\beta=0}^{2\pi} \int_{E=0}^{E_{\text{max}}} \phi'(\theta, \beta, E) \sin \theta d\theta d\beta dE$$

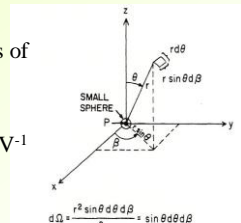


FIGURE 1.2. Polar coordinates. The element of solid angle is  $d\Omega$ .  $(x, y, z) \rightarrow (r, \theta, \beta)$

## Differential distributions: Energy spectra

- If a quantity is a function of energy only, such distribution is called the *energy spectrum* (e.g.  $\phi(E)$ )
- Typical units are  $\text{m}^{-2} \text{s}^{-1} \text{keV}^{-1}$  or  $\text{cm}^{-2} \text{s}^{-1} \text{keV}^{-1}$
- Integration over angular variables gives flux density spectrum

$$\phi(E) = \int_{\theta=0}^{\pi} \int_{\beta=0}^{2\pi} \phi'(\theta, \beta, E) \sin \theta d\theta d\beta$$

- Similarly, may define energy flux density  $\psi'(E)$

## Differential distributions: Energy spectrum example

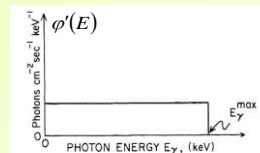


FIGURE 1.3a. A flat spectrum of photon flux density  $\phi(E)$ .

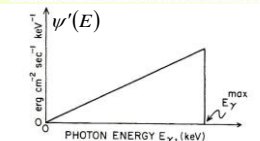


FIGURE 1.3b. Spectrum of energy flux density  $\psi'(E)$  corresponding to Fig. 1.3a.

- A “flat” distribution of photon flux density
- Energy flux density spectrum is found by

$$\psi'(E) = E\phi'(E)$$

Typically units for  $E$  are joule or erg, so that  $[\psi'] = \text{J m}^{-2} \text{s}^{-1} \text{keV}^{-1}$

## Example: Problem 1.8

An x-ray field at a point P contains  $7.5 \times 10^8$  photons/(m<sup>2</sup>-sec-keV), uniformly distributed from 10 to 100 keV.

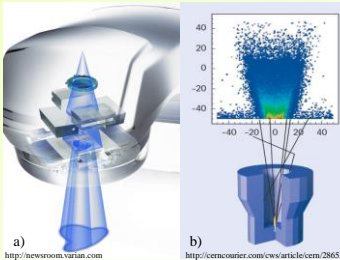
- What is the photon flux density at P?
- What would be the photon fluence in one hour?
- What is the corresponding energy fluence, in J/m<sup>2</sup> and erg/cm<sup>2</sup>?

## Example: Problem 1.8

Energy spectrum of a flux density  $\phi'(E) = 7.5 \times 10^8$  photons/m<sup>2</sup>-sec-keV

- Photon flux density  
 $\phi = \phi'(E) \cdot (E_{\max} - E_{\min}) =$   
 $7.5 \times 10^8 \cdot 90 = 6.75 \times 10^{10}$  photons/m<sup>2</sup>s
- The photon fluence in one hour  
 $\Phi(t = 1 \text{ hour}) = \phi \cdot \Delta t =$   
 $6.75 \times 10^{10} \cdot 3600 = 2.43 \times 10^{14}$  photons/m<sup>2</sup>
- The corresponding energy fluence, in J/m<sup>2</sup> and erg/cm<sup>2</sup>  
 $\Psi = \Delta t \cdot \int_{E=10}^{E=100} \phi'(E) \cdot E dE = \Delta t \cdot \phi' \cdot \frac{E^2}{2} \Big|_{10}^{100} =$   
 $3600 \cdot 7.5 \times 10^8 \cdot \frac{1}{2} (100^2 - 10^2) = 1.336 \times 10^{16}$  keV/m<sup>2</sup> =  
 $1.336 \times 10^{16} \cdot 1.602 \times 10^{-16} = 2.14 \text{ J/m}^2 = 2.14 \times 10^3 \text{ erg/cm}^2$

## Differential distributions: Angular distributions



- Full differential distribution integrated over energy leaves only angular dependence
- Often the field is symmetrical with respect to a certain direction, then only dependence on polar angle  $\theta$  or azimuthal angle  $\beta$

a) <http://newrooms.vartan.com>  
 b) <http://cerncourier.com/cws/article/cern/28653>  
 Azimuthal symmetry: a) accelerator beam after primary collimator, b) brachytherapy surface applicator

## Summary

- Types and sources of ionizing radiation
  - $\gamma$ -rays, x-rays, fast electrons, heavy charged particles, neutrons
- Description of ionizing radiation fields
  - Due random nature of radiation: expectation values and standard deviations
  - Non-stochastic quantities: fluence, flux density, energy fluence, energy flux density, differential distributions

## Quantities for Describing the Interaction of Ionizing Radiation with Matter

Chapter 2

F.A. Attix, Introduction to Radiological  
Physics and Radiation Dosimetry

## Outline

- Kerma, components of kerma
- Absorbed dose
- Exposure
- Quantities for use in radiation protection

## Introduction

- Need to describe interactions of ionizing radiation with matter
- Special interest is in the energy absorbed in matter, absorbed dose – delivered by directly ionizing radiation
- Two-step process for indirectly ionizing radiation involves kerma and absorbed dose

## Definitions

- Most of the definitions are by ICRU
- Energy transferred by indirectly ionizing radiation leads to the definition of *kerma*
- Energy imparted by ionizing radiation leads to the definition of *absorbed dose*
- Energy carried by neutrinos is ignored
  - Very small mass, no electric charge => negligibly small cross section for interactions with matter

## Energy transferred

- $\varepsilon_{tr}$  - energy transferred in a volume V to charged particles by indirectly ionizing radiation (photons and neutrons)
- *Radiant energy R* – the energy of particles emitted, transferred, or received, excluding rest mass energy
- Q - energy delivered from *rest mass* in V (positive if  $m \rightarrow E$ , negative for  $E \rightarrow m$ )

## Energy transferred

- The energy transferred in a volume V

$$\varepsilon_{tr} = (R_{in})_u - (R_{out})_u^{nonr} + \sum Q$$

↑  
uncharged

- $(R_{out})_u^{nonr}$  does not include radiative losses of kinetic energy by charged particles (bremsstrahlung or in-flight annihilation)
- Energy transferred is only the kinetic energy received by charged particles

## Kerma

- Kerma  $K$  is the energy transferred to charged particles per unit mass

$$K = \frac{d(\varepsilon_{tr})_e}{dm} \equiv \frac{d\varepsilon_{tr}}{dm}$$

- Includes radiative losses by charged particles (bremsstrahlung or in-flight annihilation of positron)
- Excludes energy passed from one charged particle to another
- Units:  $1 \text{ Gy} = 1 \text{ J/kg} = 10^2 \text{ rad} = 10^4 \text{ erg/g}$

## Relation of kerma to energy fluence for photons

- For mono-energetic photon of energy E and medium of atomic number Z, relation is through the mass energy-transfer coefficient:

$$K = \Psi \cdot \left( \frac{\mu_{tr}}{\rho} \right)_{E,Z}$$

- For a spectrum of energy fluence  $\Psi'(E)$

$$K = \int_{E=0}^{E=E_{\max}} \Psi'(E) \cdot \left( \frac{\mu_{tr}}{\rho} \right)_{E,Z} dE$$

## Energy-transfer coefficient

- Linear energy-transfer coefficient  $\mu_{tr}$ , units of  $m^{-1}$  or  $cm^{-1}$
- Mass energy-transfer coefficient  $\left(\frac{\mu_{tr}}{\rho}\right)_{E,Z}$ , units of  $m^2/kg$  or  $cm^2/g$
- Set of numerical values, tabulated for a range of photon energies, Appendix D.3

## Relation of kerma to fluence for neutrons

- Neutron field is usually described in terms of fluence rather than energy fluence
- Kerma factor is tabulated instead of kerma (units are  $rad\ cm^2/neutron$ , Appendix F)

$$(F_n)_{E,Z} = \left(\frac{\mu_{tr}}{\rho}\right)_{E,Z} \cdot E$$

- For mono-energetic neutrons

$$K = \Phi \cdot (F_n)_{E,Z}$$

## Components of Kerma

- Energy received by charged particles may be spent in two ways
  - *Collision* interactions – local dissipation of energy, ionization and excitation along electron track
  - *Radiative* interactions, such as bremsstrahlung or positron annihilation, carry energy away from the track
- Kerma may be subdivided in two components, collision and radiative:

$$K = K_c + K_r$$

- When kerma is due to neutrons, resulting charged particles are much heavier,  $K=K_c$

## Collision Kerma

- Subtracting radiant energy emitted by charged particles  $R_u^r$  from energy transferred results in *net* energy transferred locally

$$\mathcal{E}_{tr}^{net} = \mathcal{E}_{tr} - R_u^r = (R_{in})_u - (R_{out})_u^{nonr} - R_u^r + \sum Q$$

- Now collision kerma can be defined

$$K_c = \frac{d\mathcal{E}_{tr}^{net}}{dm}$$

## Mass energy-absorption coefficient

- Since collision kerma represents energy deposited (absorbed) locally, introduce mass energy-absorption coefficient. For mono-energetic photon beam

$$K_c = \Psi \cdot \left(\frac{\mu_{en}}{\rho}\right)_{E,Z}$$

- Depends on materials present along particle track before reaching point P

## Mass energy-absorption coefficient

- For low Z materials and low energy radiative losses are small, therefore values of  $\mu_{tr}$  and  $\mu_{en}$  are close

$\gamma$ -ray Energy (MeV)	$100(\mu_{tr} - \mu_{en})/\mu_{tr}$		
	Z = 6	29	82
0.1	0	0	0
1.0	0	1.1	4.8
10	3.5	13.3	26

## Kerma rate

- Kerma rate at point P and time  $t$

$$\dot{K} = \frac{dK}{dt} = \frac{d}{dt} \left( \frac{d\mathcal{E}_{ir}}{dm} \right)$$

- Units of J/(kg s), erg/(g s), or rad/s
- Knowing kerma rate, kerma

$$K(t_0, t_1) = \int_{t_0}^{t_1} \dot{K}(t) dt$$

## Absorbed dose

- Energy imparted by ionizing radiation to matter of mass  $m$  in volume  $V$

$$\mathcal{E} = \underbrace{(R_{in})_u}_{\text{due to uncharged}} - \underbrace{(R_{out})_u}_{\text{due to uncharged}} + \underbrace{(R_{in})_c}_{\text{due to charged}} - \underbrace{(R_{out})_c}_{\text{due to charged}} + \sum Q$$

- Absorbed dose is defined as

$$D = \frac{d\mathcal{E}}{dm}$$

- Units: 1 Gy = 1 J/kg =  $10^2$  rad =  $10^4$  erg/g

## Absorbed dose

- $D$  represents the energy per unit mass which remains in the matter at P to produce any effects attributable to radiation
- The most important quantity in radiological physics
- Absorbed dose rate:

$$\dot{D} = \frac{dD}{dt} = \frac{d}{dt} \left( \frac{d\mathcal{E}}{dm} \right)$$

## Example 1

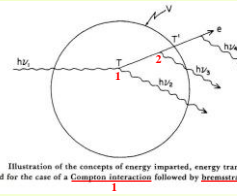


FIGURE 2.1a. Illustration of the concepts of energy imparted, energy transferred, and net energy transferred for the case of a Compton interaction followed by bremsstrahlung emission (Attix, 1983).

$$\text{Energy imparted} \quad \mathcal{E} = (R_{in})_u - (R_{out})_u + (R_{in})_c - (R_{out})_c + \sum Q$$

$$\text{Energy transferred} \quad \mathcal{E}_{tr} = (R_{in})_u - (R_{out})_u^{nonr} + \sum Q$$

$$\text{Net energy transferred} \quad \mathcal{E}_{tr}^{net} = (R_{in})_u - (R_{out})_u^{nonr} - R'_u + \sum Q$$

## Example 1

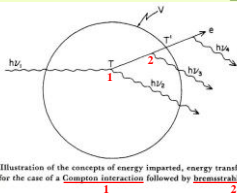


FIGURE 2.1a. Illustration of the concepts of energy imparted, energy transferred, and net energy transferred for the case of a Compton interaction followed by bremsstrahlung emission (Attix, 1983).

$$\text{Energy imparted} \quad \mathcal{E} = (R_{in})_u - (R_{out})_u + (R_{in})_c - (R_{out})_c + \sum Q$$

$$\text{Energy transferred} \quad \mathcal{E}_{tr} = (R_{in})_u - (R_{out})_u^{nonr} + \sum Q$$

$$\text{Net energy transferred} \quad \mathcal{E}_{tr}^{net} = (R_{in})_u - (R_{out})_u^{nonr} - R'_u + \sum Q$$

$$\begin{aligned} (R_{in})_u &= h\nu_1 \\ (R_{out})_u &= (R_{out})_u^{nonr} = h\nu_2 \\ (R_{in})_c &= 0, \quad Q = 0 \\ (R_{out})_c &= h\nu_3 + T' \\ R'_u &= h\nu_3 \end{aligned}$$

## Example 1

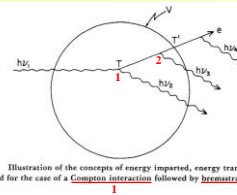


FIGURE 2.1a. Illustration of the concepts of energy imparted, energy transferred, and net energy transferred for the case of a Compton interaction followed by bremsstrahlung emission (Attix, 1983).

$$\mathcal{E} = h\nu_1 - (h\nu_2 + h\nu_3 + T') + 0$$

$$\mathcal{E}_{tr} = h\nu_1 - h\nu_2 + 0 = T$$

$$\begin{aligned} \mathcal{E}_{tr}^{net} &= h\nu_1 - h\nu_2 - h\nu_3 + 0 \\ &= T - h\nu_3 \end{aligned}$$



## Example 2

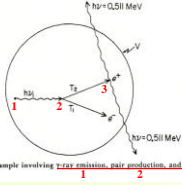


FIGURE 2.1A. Example involving  $\gamma$ -ray emission, pair production, and positron annihilation (Attix, 1983).

Positron has no excess kinetic energy to transfer to photons after annihilation

$$\text{Energy imparted} \quad \mathcal{E} = (R_{in})_u - (R_{out})_u + (R_{in})_c - (R_{out})_c + \sum Q$$

$$\text{Energy transferred} \quad \mathcal{E}_{tr} = (R_{in})_u - (R_{out})_u^{nonr} + \sum Q$$

$$\text{Net energy transferred} \quad \mathcal{E}_{tr}^{net} = (R_{in})_u - (R_{out})_u^{nonr} - R_u^r + \sum Q$$

## Example 2

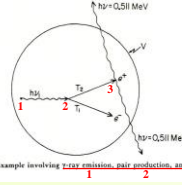


FIGURE 2.1A. Example involving  $\gamma$ -ray emission, pair production, and positron annihilation (Attix, 1983).

Positron has no excess kinetic energy to transfer to photons after annihilation

$$(R_{in})_u = (R_{in})_c = (R_{out})_c = R_u^r = 0$$

$$(R_{out})_u = (R_{out})_u^{nonr} = 2h\nu = 1.022\text{MeV}$$

$$\sum Q = h\nu_1 - 2m_0c^2 + 2m_0c^2 = h\nu_1$$

$$\mathcal{E} = \mathcal{E}_{tr} = \mathcal{E}_{tr}^{net} = h\nu_1 - 1.022\text{ MeV} = T_1 + T_2$$

## Example 3

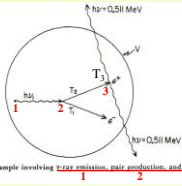


FIGURE 2.1A. Example involving  $\gamma$ -ray emission, pair production, and positron annihilation (Attix, 1983).

- Positron transfers excess kinetic energy  $T_3$  to photons after annihilation.
- It generates radiative loss from charged-particle kinetic energy
- Affects  $\mathcal{E}$  and  $\mathcal{E}_{tr}^n$  by subtraction of  $T_3$

$$(R_{in})_u = (R_{in})_c = (R_{out})_c = 0$$

$$(R_{out})_u = 2h\nu + T_3 = 1.022\text{MeV} + T_3$$

$$(R_{out})_u^{nonr} = 2h\nu = 1.022\text{MeV}$$

$$R_u^r = T_3$$

$$\sum Q = h\nu_1 - 2m_0c^2 + 2m_0c^2 = h\nu_1$$

## Exposure

- Historically, was introduced before kerma and dose, measured in roentgen (R)
- Defined as a quotient

$$X = \frac{dQ}{dm}$$

- $dQ$  is absolute value of the total charge of the ions of one sign produced in air when all electrons liberated by photons in air of mass  $dm$  are completely stopped in air
- Ionization from the absorption of radiative loss of kinetic energy by electrons is *not included*

## Exposure

- Exposure is the ionization equivalent of the collision kerma in air for x and  $\gamma$ -rays
- Introduce mean energy expended in a gas per ion pair formed,  $\bar{W}$ , constant for each gas, independent of incoming photon energy
- For dry air

$$\frac{\bar{W}_{air}}{e} = \frac{33.97\text{ eV/i.p.}}{1.602 \times 10^{-19}\text{ C/electron}} \times 1.602 \times 10^{-19}\text{ J/eV} = 33.97\text{ J/C}$$

## Relation of exposure to energy fluence

- Exposure at a point due to energy fluence of mono-energetic photons

$$X = \Psi \cdot \left( \frac{\mu_{en}}{\rho} \right)_{E,air} \left( \frac{e}{\bar{W}} \right)_{air} =$$

$$(K_c)_{air} \left( \frac{e}{\bar{W}} \right)_{air} = (K_c)_{air} / 33.97$$

- Units of  $[X] = \text{C/kg}$  in SI

## Units of exposure

- The roentgen R is the customary unit
- The roentgen is defined as exposure producing in air one unit of esu of charge per 0.001293 g of air irradiated by the photons. Conversion

$$1R = \frac{1\text{esu}}{0.001293\text{g}} \times \frac{1\text{C}}{2.998 \times 10^9\text{esu}} \times \frac{10^3\text{g}}{1\text{kg}}$$

$$= 2.580 \times 10^{-4}\text{C/kg}$$

$$1\text{C/kg} = 3876\text{R}$$

## Exposure rate

- Exposure rate at a point P and time t:

$$\dot{X} = \frac{dX}{dt}$$

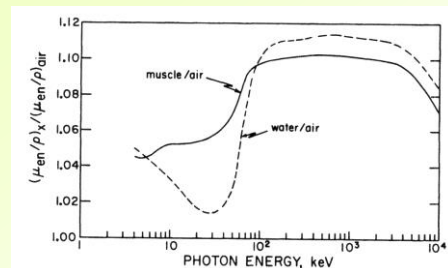
- Units are C/(kg-sec) or R/sec
- Exposure

$$X = \int_{t_0}^{t_1} \dot{X}(t) dt$$

## Significance of exposure

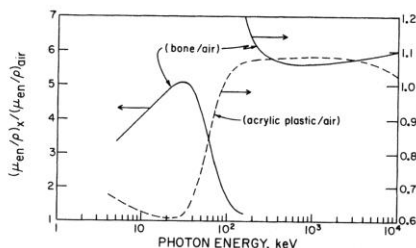
- Energy fluence is proportional to exposure for any given photon energy or spectrum
- Due to similarity in effective atomic number
  - Air can be made a tissue equivalent medium with respect to energy absorption – convenient in measurements
  - Collision kerma in muscle per unit of exposure is nearly independent of photon energy

## Significance of exposure



Ratio of mass energy-absorption coefficients for muscle/air and water/air are nearly constant (within <5%) for energies from 4keV to 10 MeV

## Significance of exposure



Ratio of mass energy-absorption coefficients for bone/air and acrylic/air are nearly constant for energies above 100keV

## Significance of exposure

- X-ray field at a point can be characterized by means of exposure regardless of whether there is air actually located at this point
- It implies that photon energy fluence at that point is such that it would produce exposure of a stated value
- Same is applicable to kerma or collision kerma, except that reference medium (not necessarily air) has to be specified

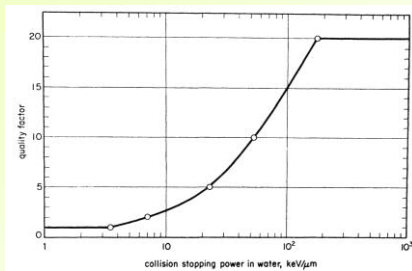
## Radiation protection quantities

- Dose equivalent  $H$ , is defined as
$$H \equiv DQN$$
- Here  $D$  – dose,  $Q$ - quality factor,  $N$ -product of modifying factors (currently=1)
- Units of  $H$ :
  - severs,  $Sv$ , if dose is expressed in  $J/kg$
  - $rem$ , if dose is in  $rad$  ( $10^{-2} J/kg$ )

## Radiation protection quantities

- Quality factor  $Q$  – weighting factor to be applied to absorbed dose to provide an estimate of the relative human hazard of ionizing radiation
- It is based on relative biological effectiveness (RBE) of a particular radiation source
- $Q$  is dimensionless

## Radiation protection quantities



- Higher-density charged particle tracks (higher collision stopping power) are more damaging per unit dose

## Summary

- Quantities describing the interaction of ionizing radiation with matter
  - Kerma, components of kerma
  - Absorbed dose
  - Exposure
- Relationship with fluence and energy fluence
- Quantities for use in radiation protection